Does it count?

- embedding CAA in an effective way

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A dilemma

- 1. Students do things only for marks (from school?)
- 2. They work to the next test only (even missing lectures!)
- 3. So individual lecturers need to set plenty of assessments in order to get their share of students' attention/ engagement (else they fail the module)
- 4. So students have no time for reflection and understanding
- 5. Go to 1) above!

Result: the course is no fun!

CAA at Brunel University

- Javascript, MathML, SVG, web delivery
- Questions database spans GCSE, A-level, undergraduate topics, ADULT LEARNERS/employability aptitude
- >3500 questions in the database span MC, NI, RNI, PNI, TFU, MR, NI+confidence, Revealed MC, drag&drop etc. (no free-form maths input ... yet): PROS/CONS?
- Hundreds of users take circa 30,000 tests p.a. Students from Maths, Economics, Electrical and Electronic Engineering, Computing, Foundations of Engineering, Foundations of IT, PGCE and Sports Science, even MSc student diagnostics. Much commonality

1 of 1

This week Mavis slarled her new job as a sales assistant in a huge loy slore. The pictogram below shows the number of loys she sold in her first week.

Monday							
Tuesday							
Wednesday							
Thursday							
Friday							
(ey: epresents a box of 20 toys.							
low many toys did Mavis sell on Thursday?							
Submit							
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Adult numeracy?

- Pictogram changes
- Scenario changes
- Notice the key -> malrule
- 50% of British adults have the numeracy skills required of a 7year old ... a skills shortage that is holding back the economy

🍓 Question M

CAA in practice - a way out?

- Low-stakes summative assessment invigilated or not.
- Preferred scheme: best-ever mark from their first 5 attempts counts towards their module mark; not invigilated and group work is allowed/encouraged.
 <u>Exam pass required!</u>
- Blended assessment (CAA, traditional exams, labs, reports & essays ...) Why drive a car?
- Mostly we aim to promote learning ... we don't really need more marks!

MATHS TESTS 1-5 Prices Currently Other Tests - £5 Matrices Part 1 - £10 Matrices Part 2 - £10 .All 5 tests = $\pounds 30$ (save $\pounds 5$) Flexible Availability - Living on Campus rested SC Milen Yadav 0 **Milen Yadav**

2 slots available, prices will rise closer to the deadline 13:47

PM ME If Interested, all you need to provide is your computer login and a picture of the results will be sent through both Whatsapp and Email.

13:53

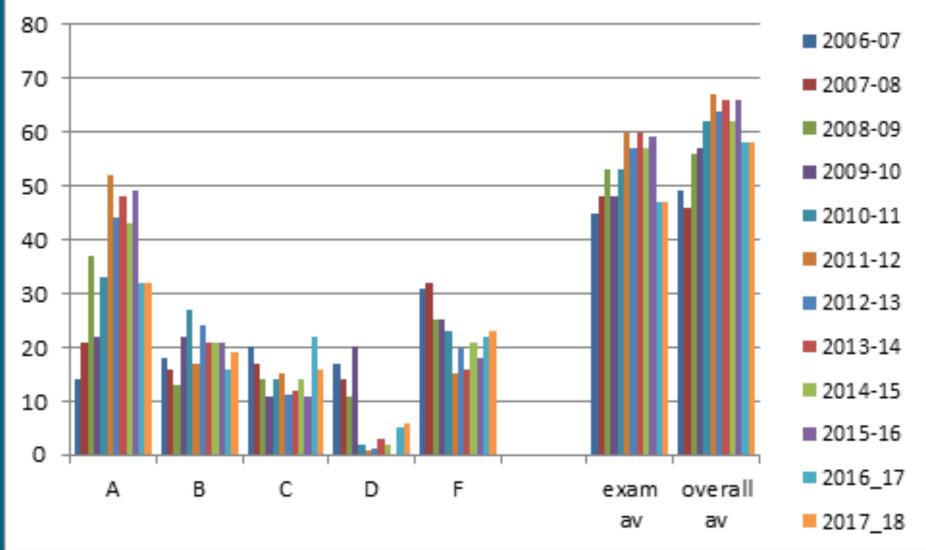
Mathematics for Economics (year-by-year changes in assessment)

2006/07, 2007/08:no CAA; A and non-A cohorts – results
indistinguishable; two class tests, one 3-hour
economics staff (10 days - times 2?)exam set by
exam set by
economics for all concerned!2008/09:CAA introduced; 3-hour exam only
(4 days)

2009/10, 2010/16: one cohort, admission AS level mathematics; exam pass mandatory; 2-hour exam only (set by MG to 2015) (3 days)

20016/17, 2017-18: one cohort, admission **GCSE** mathematics; exam pass mandatory; 2-hour exam only (set by MW since 2015) **(3 days)**

Maths for Economics year-on-year results (% in grade/% mark) circa 500,000 questions done



Effective learning + Economies?

• From Teaching Mathematics and Its Applications doi:10.1093/teamat/hrv012

Simplifying the logistics of setting tests, particularly incourse or continuous assessment tests of large cohorts (up to several hundred in an HE context). Depending on the embedding scenario chosen (see below), CAA can remove many of the administration tasks such as timetabling, booking rooms, informing students, making arrangements for students with special needs, repeat tests for those unable to do the first test instance. . . and finally the whole process again for resit tests.

Effective teaching /economies!

Endless source of reverse-engineered questions useful for lecture notes, problem sheets (if used) and first part of exam questions, followed perhaps by objective open questions to do with:

Modelling,

Proof

Interpretation

Critiquing

Extension ...

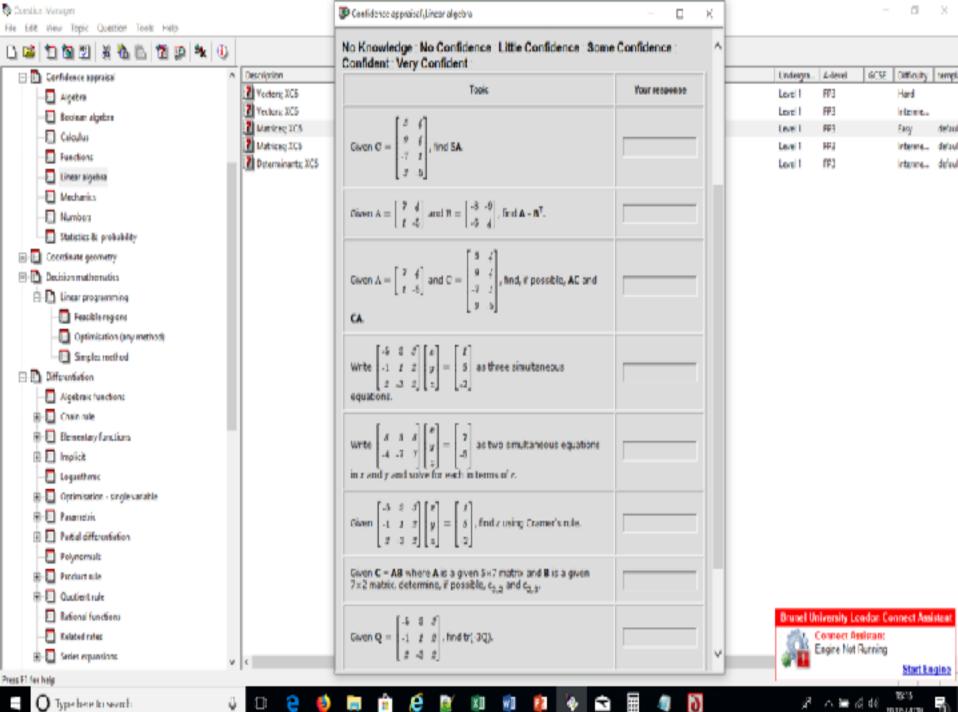
MCQs a bad image?

- MCQs merely ask students to spot the correct answer when they see it.
- They are very heavily 'scaffolded' with the key and distracters suggesting the form or size of the answer, e.g., not taking the square root of the variance would give a distracter that is unrealistically large for the standard deviation.
- Partial knowledge may eliminate some distracters and encourage guessing, for example by using symmetry (a good skill, but probably not the one intended to be tested by the question).
- Trial values such as x=0, 1, 2 . . . might be used until all but the correct answer is eliminated.
- The question might be done backwards, e.g., differentiating all the options rather than integrating the integrand in the question.
- Pattern spotting might be employed where the student looks for commonality in parts of the options. For example, what are the coordinates of a calculated point in space, with options (1,1,1), (1,1,0), (1,0,1) and (0,1,1) suggest that (1,1,1) is the correct answer.

But they BUILD CONFIDENCE!

- Example: Differentiate cos(2x)
- Mal-rules? Pick up usual errors easily ...

Differentiate cos(x²) ... needs a human to explain? Well maybe not!



10.05.6010

Algebra/Vigebraic fractions/Partial fractions/Irreducible factors/Quadratic & guadratic

1 of 1

Bruce is trying to decompose the following rational function into the sum of partial fractions, but he may have made a mistake

If there is a mistake in Bruce's workings shown below, in which line was the mistake first made?

 $\frac{10x^3 - 26x^2 - 8x - 8}{-8x^4 + 2x^3 - 23x^2 + 12x - 15} = \frac{10x^3 - 26x^2 - 8x - 8}{(-2x^2 - x - 5)(4x^2 - 3x + 3)}$ $\frac{10x^3 - 26x^2 - 8x - 8}{8x^4 + 2x^2 - 23x^2 + 12x - 15} = \frac{Ax + B}{(-2x^2 - x - 5)} + \frac{Fx + G}{(4x^2 - 3x + 3)}$

line 3:
$$10x^3 + 26x^2 + 8x + 8 = (Ax + B)(4x^2 + 3x + 3) + (Fx + G)(-2x^2 + x + 5)$$

line 4: $10 = 4\Lambda - 2\Gamma$ line 5: $-26 = -3\Lambda + 4B - \Gamma - 2C$

mee. -10 - -011 | -10 - 1 - 14

 $\operatorname{Inc} 6^\circ$ -8 \pm 3A \pm 3B \pm 5F \pm C

line / $-8 = 3B_{2}5G$

```
\log \otimes \bigcirc A=5, B=-1, F=5 \text{ and } G=1
```

Reverse engineering But do we want them to do this? Will they use Wolfram alpha? Yep!

17 ×

Colours sature

& Fonts

Part this screen

 $\lim u = \frac{10x^2 - 26x^2 - 8x - 8}{-8x^4 + 2x^3 - 23x^2 + 12x - 15} = \frac{5x + 1}{(-2x^2 - x - 5)} + \frac{5x - 1}{(4x^2 - 3x + 3)}$

Wease reput the line relation where the metallic test means, or input 0 if there is no mistake

The		1- 1- I	line	L
Ine	error	15 IN I	ine	L

Preferable? TF(U) question

A positive quantity Q is known to depend on two positive variables as follows:

Mathematically we can write this as $g = e^{-\frac{x}{g^3}}$

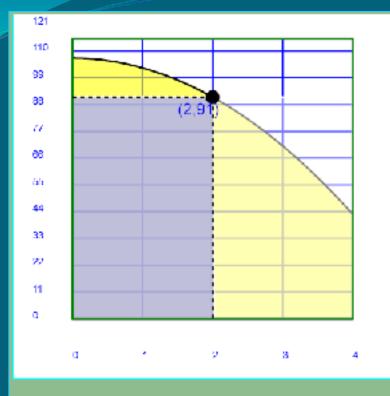
The following claims are made.

If you think the claim is **true, input T** It you think the claim is **false, input F**. If you think the claim is **undecidable** on the basis of the information given, ir

Claim	T, For U ?
If <i>R</i> decreases and <i>S</i> increases, <i>Q</i> decreases.	
If R decreases and B decreases, Q stays the same.	
If <i>R</i> decreases and <i>S</i> stays the same, <i>Q</i> increases.	
If R increases and S decreases, Q decreases.	

• Tests

- understanding (I think ...)
- This question context (not fully shown) makes it clear that k > 0
- What if k < 0 ?



The consumer surplus is given by the yellow area in the above graph, this is the definite integral under the curve from 0 to 2 minus the area of the blue rectangle of height 91 and width 2 i.e.

$$\begin{split} \mathbf{CS} &= \int_{0}^{0} \left[0 \mathcal{C} - \mathcal{C} \mathcal{G}^{2} \right] \, d\mathcal{G} \qquad 9^{*} \times 0 \\ &= \left[1 0 \mathcal{C} \mathcal{G} - \frac{2 \mathcal{G}^{2}}{2} \right]_{0}^{2} \qquad 2 n \mathcal{C} = \mathcal{C} 1 + \mathcal{C} . \end{split}$$

Feedback contextualised

- economics question
- part of the formative feedback
- SVG diagram realised according to the random parameters in the question
- related material button
 links to any web
 resource (via centrallyheld lookup array)

Related material

Economics/Interest/Investment appraisal/Sinking funds, annutics & perpetuties.

Demand for oil is currently 59000 billion units per year, but is set to fall by 13% annually. If current world stocks stand at 393000 billion units, after how many years will this resource completely exhausted?

L

×

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-----Your result-----

Your answer 333 years, should have been 15.

At the end of the year 1 we will have used 59000 units.

At the end of the year 2 we will have used another 59000(1-0.13) units.

At the end of the year 3 we will have used another 59000(1-0.13)² units.... and so on until

At the end of the year n we will have used another 59000(1-0.13)ⁿ⁻¹ units.

Adding these up gives the series:

 $59000 + 59000(1 - 0.13)^{1} + ... + 59000(1 - 0.13)^{n-1}$

i.e. a geometric progression with first term 59000

common ratio (1 - 0.13)

and the number of terms is n which you needed to find.

Using the general formula for the sum of a G.P. $S_n = rac{a\,(r^n-1)}{r-1}$

Setting this equal to the world reserves gives $\frac{59000(0.87^n-1)}{0.87-1} = 393000$

To solve this for *n* we need to simplify: $(0.87^n - 1) = \frac{393000(0.87 - 1)}{59000} \approx -0.865932$

Adding 1 to both sides and taking logs gives: $n = \frac{\log(0.134068)}{\log(0.87)} = 14.428970$

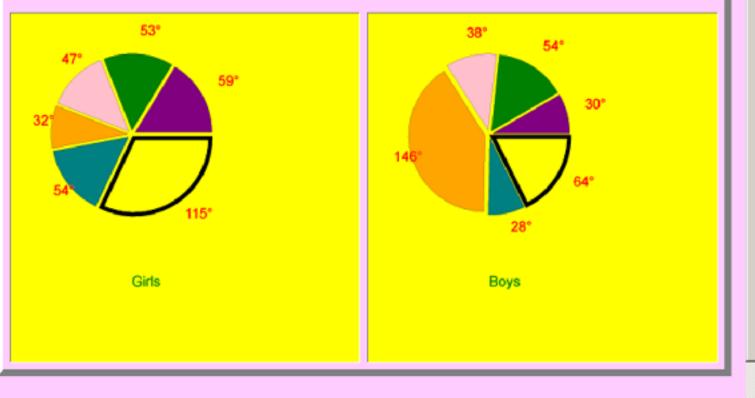
so we have completely exhausted the world reserves of oil after 15 years.

DeSTRESS JISC Project

- Builds on the Metal question design methodology and experiences to test basic stats for social sciences
- Released new material end August 2011
- Hand calculation with realistically-sized data sets solution to link with external software such as Excel, SPSS
- Real data? Data cannot be 'designed' to have certain features or not. Problems with keeping the data and answers current without accessing live web sites (problems of access and communication with the marking scheme).
- Another challenging area is the interpretation of charts and graphs

George works for an exam board and is looking at the GCSE maths results. He wants to examine any gender bias by taking 300 candidates of each gender. The results are presented in the pie charts below. (Due to rounding, at times the values around the pie chart may not add to 360°)





Calculate the difference in number between girls and boys who achieved grade F.

Round your final answer to the nearest whole number.

Descriptive stats ... lots of randoms here including stated grade and dynamic diagrams via SVG

Copy to Clipboard

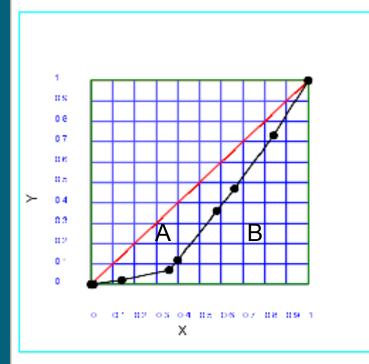
The table below gives income data i.e. coordinates on the Lorentz curve for a certain country. Calculate the Gini coefficient assuming linear

Cumulative percent of households	1	14	36	40	58	66	84	100
Cumulative share of national income	0	2	7	12	36	47	73	100

😴 Farmonics applications?PersontagerMules rumbers

The Gini coefficient is the ratio of the area A above the black Lorentz curve (actually a ploygen here) and below the red line of equality (which has area = 1/2 i.e. the area of the triangle of width and height 1). This is then simply 2A. The curves are shown below. The line of equality is when everyone gets the same income and then C = 0. At the other extreme, suppose just one household gets all the national income (of a large population) then the Lorentz curve would be alone the x axis unblix. If when it would shoot up to y=1. That curve would have no area underneath it so A would equal 1/2 and C would then be 1.

Small Gini coefficients therefore imply a more equal society, although the income Gini coefficient has nothing to do with the wealth distribution - for that we would need different data and then calculate the wealth Gini coefficient. Typically under-developed countries have larger income and wealth Gini coefficients where the money is in the hands of an eitle whitat the majority of the population lives in relative poverty. However, note the word *colabve* here; the Gini coefficient tells us nothing about absolute standards of income, merely how equal incomes are (or not). In the UK the income Gini coefficient has increased rapidly to the present date (August 2011) and one could ask if this is at least partly related to recent rioling!



Gini coefficient G = A/(A+B) = 2A _ T 🔀

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A statistics question - tables or formula?

🖉 Statistics/Distributions/Himmial/Coundatine probability/Decoutextual/by formula or 4dp tables 🗉

From the Cumulative Binomial distribution table below find and click the probability stated below, where X follows a binomial distribution and has the given value of n. The table below provides corresponding probabilities for X less than or equal to stated values of x.

You can choose your answer from the Binomial distribution table by clicking your mouse. You will not be able to change your mind after you click on an answer, so make sure you choose your answers carefully before clicking. This question holds 2 marks, where full marks can be achieved by selecting the correct answer at the first attempt.



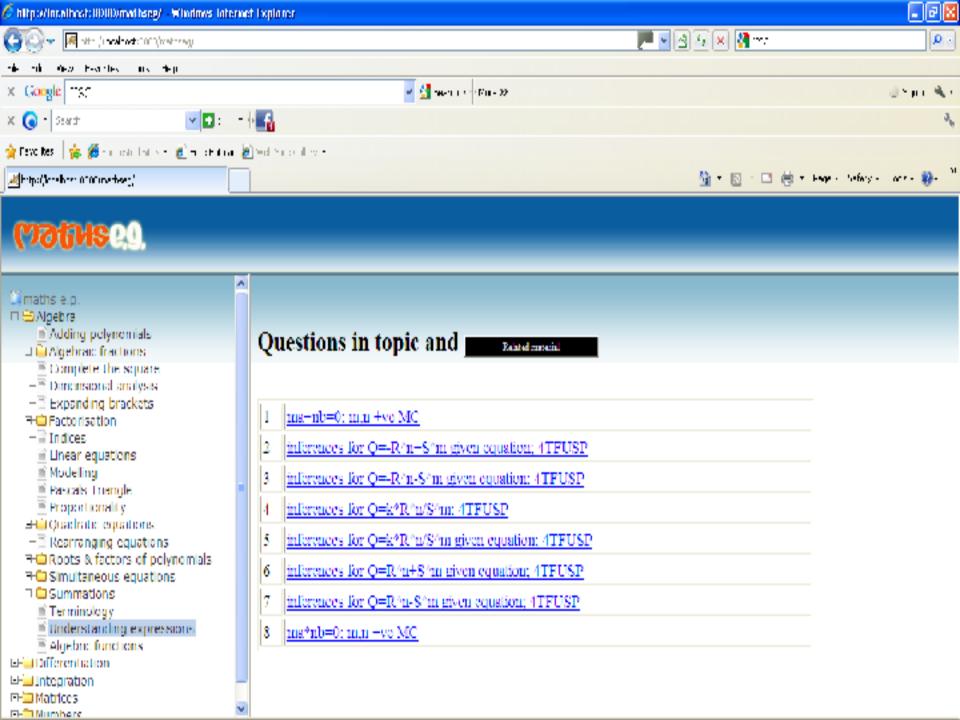
Table



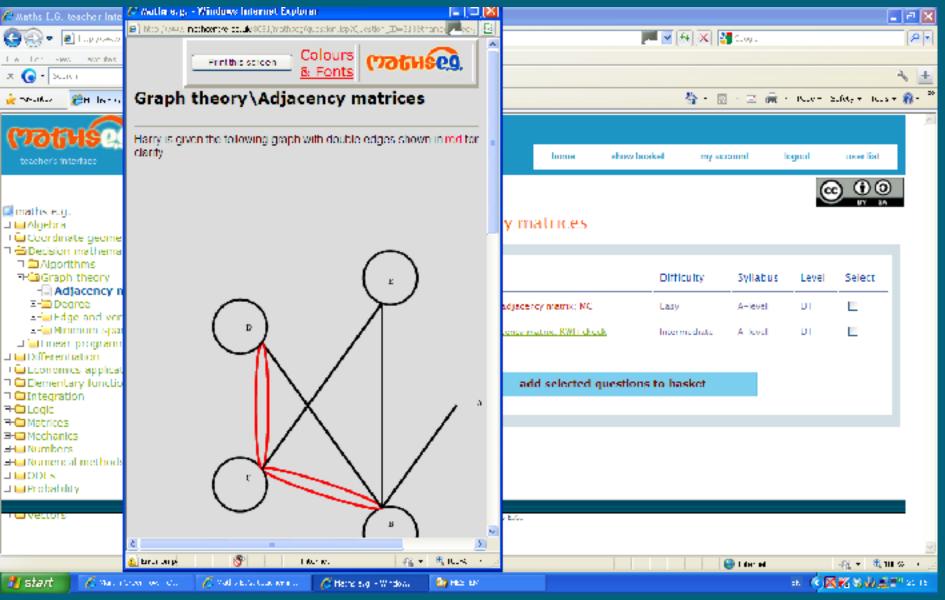
d X

 $F(X \le 10 | n = 0.25)$ has the value of (click on the table)

P=	0.05	0.1	0.15	0.2	0.25	0.3	0.35	0.4	0.45	0.5
n=5,x=0	0.7738	0.5905	0.4437	0.3277	0.2373	0.1681	0.116	0.0778	0.0503	0.0312
1	0.9774	0.9185	0.8352	0.7373	0.6328	0.5282	0.4284	0.337	0.2562	0.1875
2	0.9988	0.9914	0.9734	0.9421	0.8965	0.8369	0.7648	0.6826	0.5931	0.5
3	1	0.9995	0.9978	0.9933	0.9844	0.9692	0.946	0.913	0.8688	0.8125
4	1	1	0.9999	0.9997	0.999	0.9976	0.9947	0.9898	0.9815	0.9688
n=10,x=0	0.5987	0.3487	0.1969	0.1074	0.0563	0.0282	0.0135	0.006	0.0025	0.0025
1	0.9139	0.7361	0.5443	0.3758	0.244	0.1493	0.086	0.0464	0.0233	0.0233
2	0.9885	0.9298	0.8202	0.6778	0.5256	0.3828	0.2616	0.1673	0.0996	0.0996
2	n 000	0 0872	0.05	0.8701	0 7750	0.6405	0.5129	0.2822	0.266	0.266
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Teacher interface — shop on Amazon?



Javascript, MathML and SVG provide a rich environment for setting objective questions

Positive effects on students' perceptions and on exam performances

➤ Widely applicable database of questions

➤Good source of reverse-engineered questions for all, especially teachers

 \succ Maths e.g. Try it at:

http://www.mathcentre.ac.uk:8081/mathseg/

http://www.mathcentre.ac.uk:8081/mathsegteacher/

works on all browsers, PC & Mac, I-pads and smart phones, no link to VLEs yet!

Where are we going with all this?

Can we get systems to share or work together? Future-proofing?